

Advanced Structural Geology, Fall 2022

# Simple Deformation

Ramón Arrowsmith

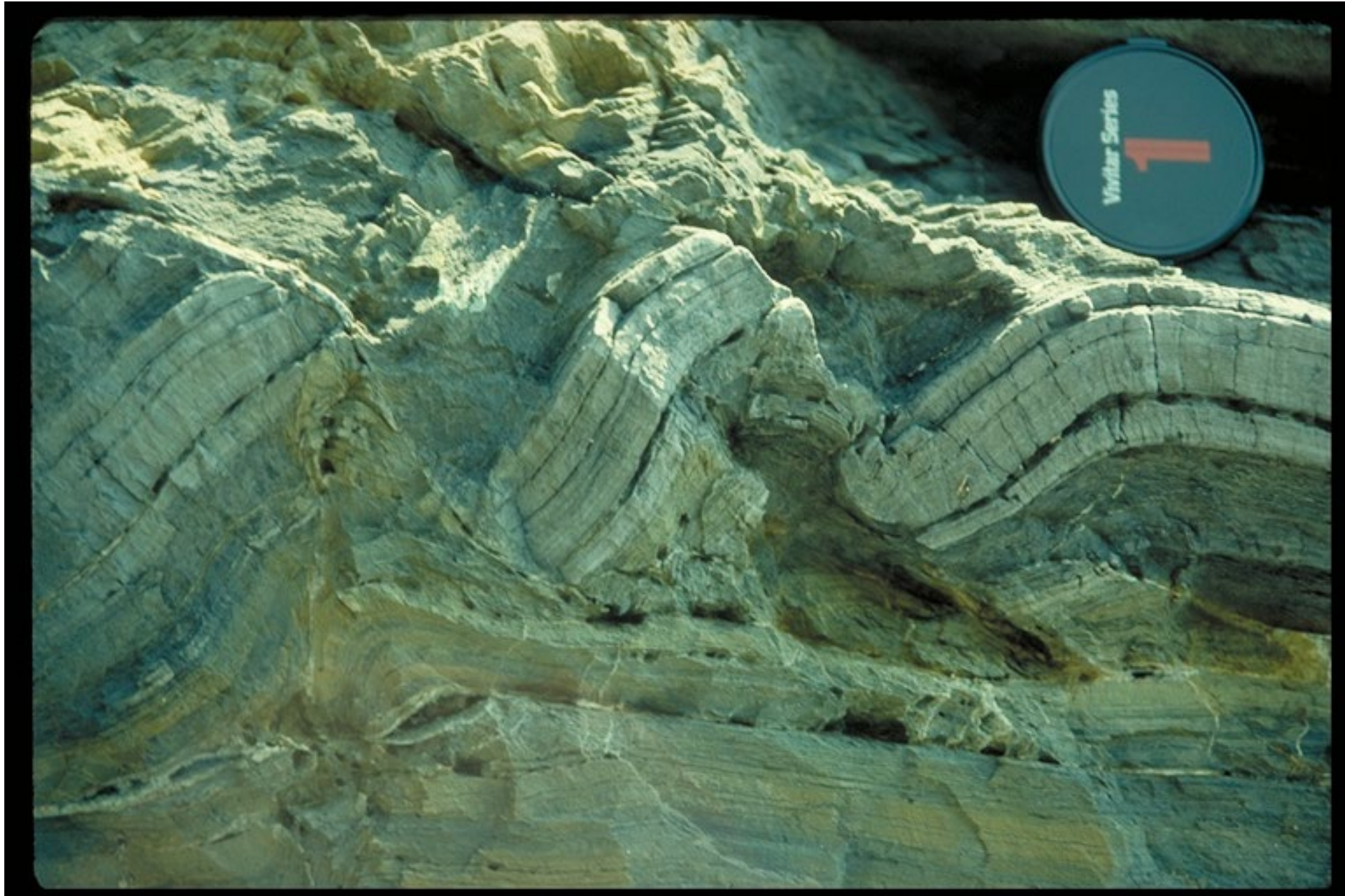
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Just how deformed is this rock?



Or this one?

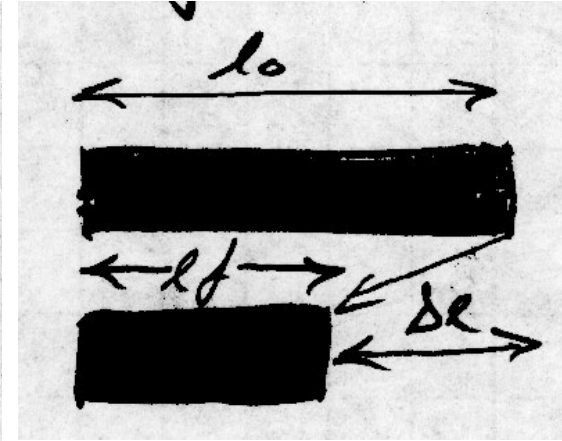
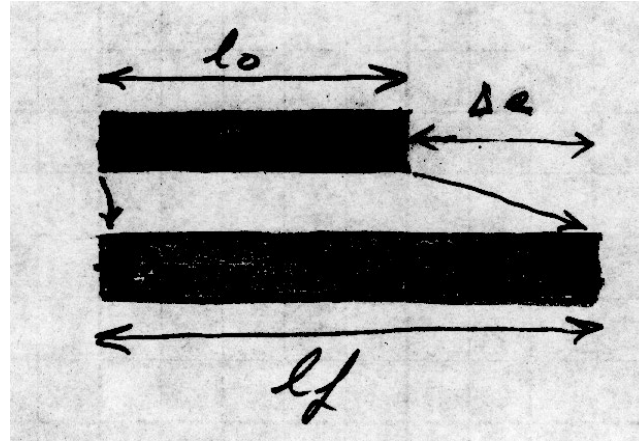


# Summary of measures of deformation by changes in lengths of lines

Extension or elongation;

$$e = (l_f - l_o) / l_o$$

where  $l_o$  = initial length and  $l_f$  = final length



Stretch;

$$S = l_f / l_o \text{ or } s = 1 + e$$

“Extension”

$$l_f > l_o, \text{ so } e = >0 / l_o > 0$$

$$S = l_f / l_o > 1$$

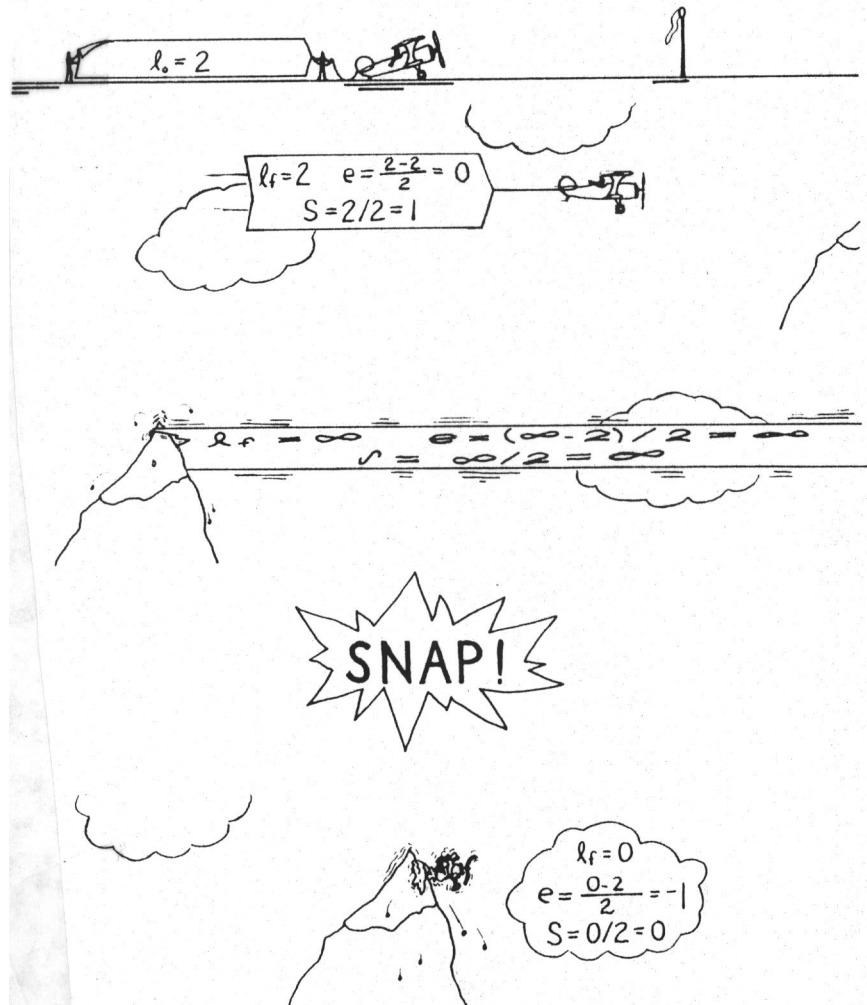
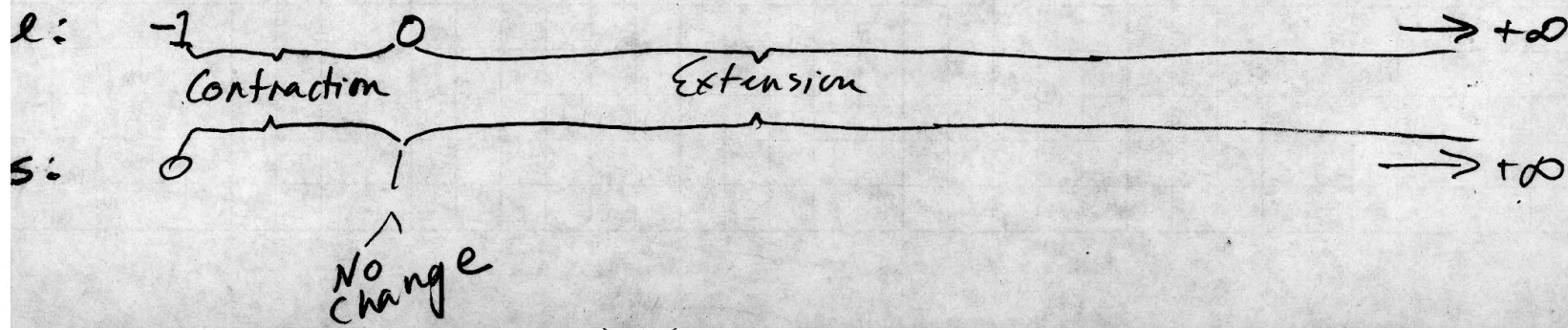
“Shortening”,

“Contraction”, “Negative extension”

$$l_f < l_o, \text{ so } e = <0 / l_o < 0$$

$$S = l_f / l_o < 1$$

But, when  $l_f = 0$ ,  $e = \frac{0 - l_o}{l_o} = \frac{-l_o}{l_o} = -1$   
 and  $s = \frac{l_f}{l_o} = \frac{0}{l_o} = 0$

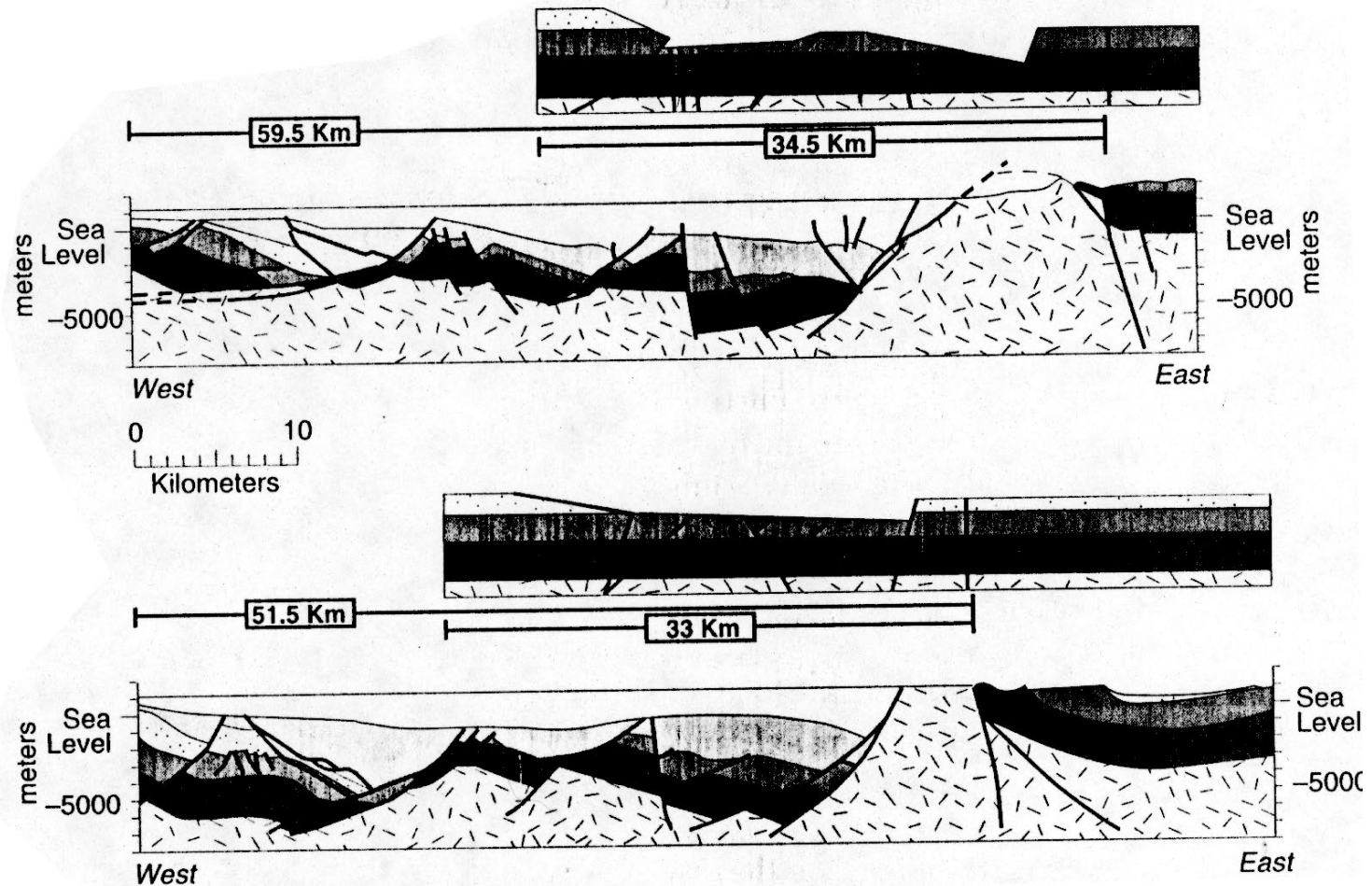
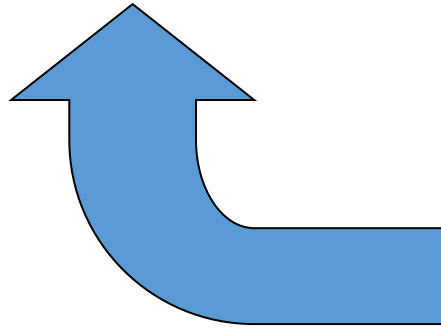


**Figure 2.30** The ribbonlike banner that is neither stretched nor shortened has an  $e$  value of zero and an  $S$  value of 1.0. If the banner is stretched toward infinite length, both its  $e$  and  $S$  values approach infinity. If the banner is shortened toward zero, its  $e$  value approaches  $-1$  and its  $S$  value approaches 0. On this particular flight, the airplane to which the banner is attached undergoes non-rigid deformation. (Artwork by R. W. Krantz.)

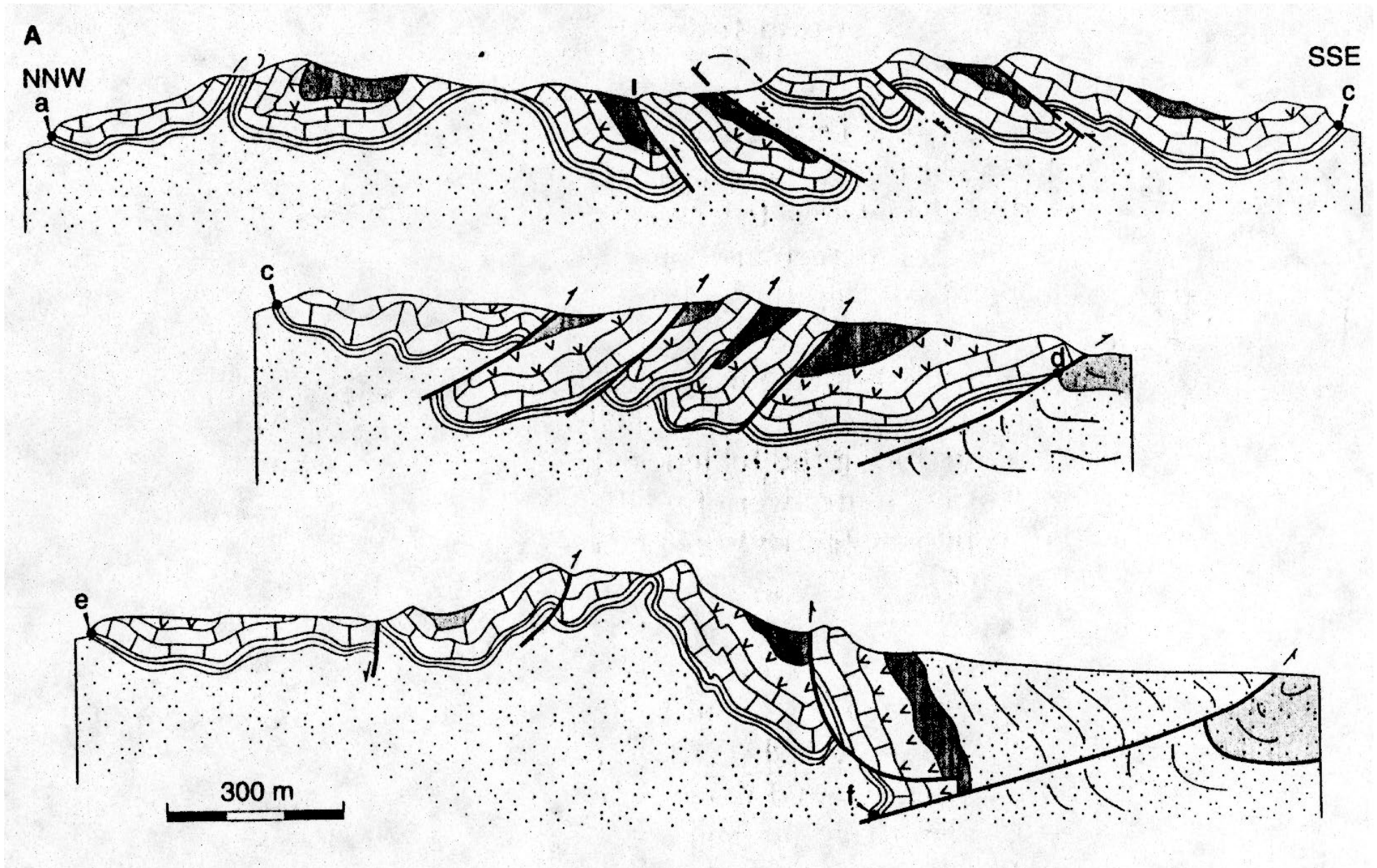
# Change in length of region because of faulting

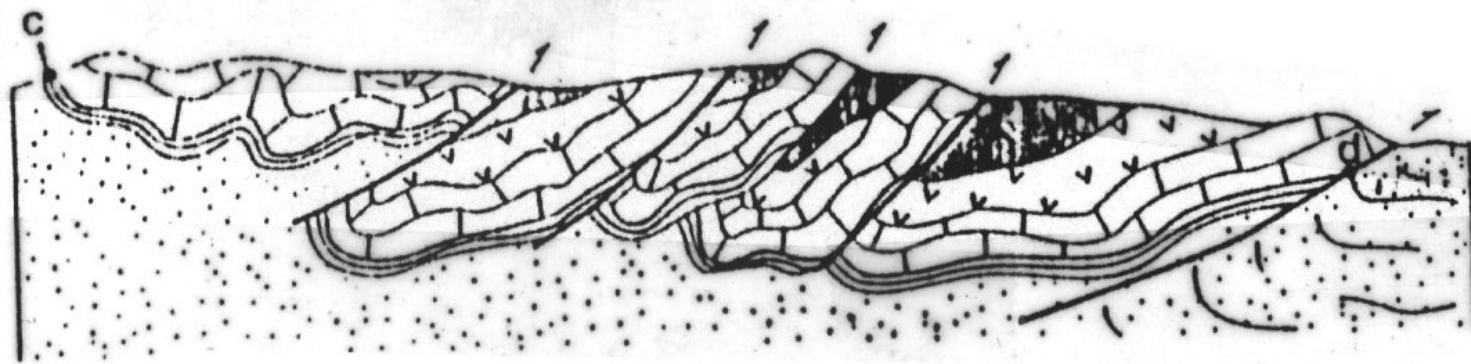
$$e = (l_f - l_o) / l_o = (59.5 - 34.5) / 34.5 = 25 / 34.5 = 0.72$$

$$s = l_f / l_o = 59.5 / 34.5 = 1 + e = 1.72$$

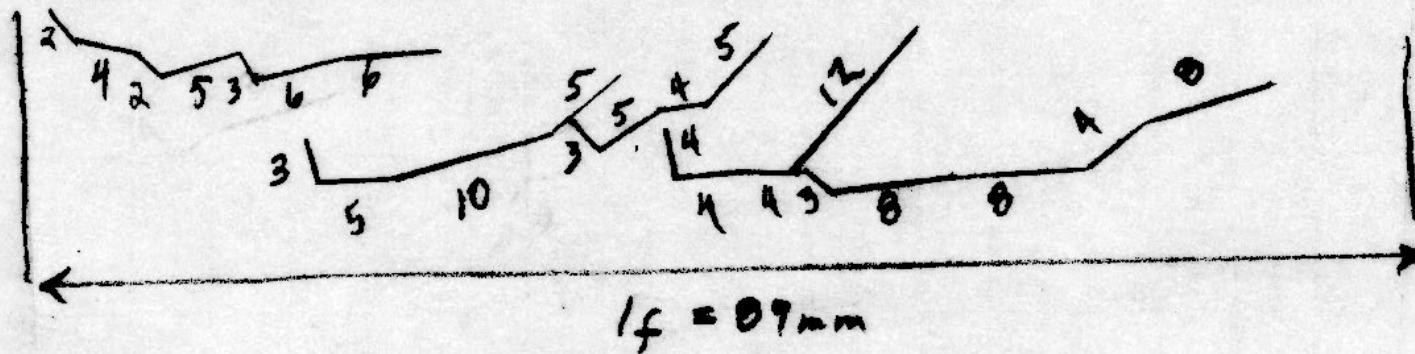


Is  $e < 0$  or  $> 0$ ?





Line 5 represents approximately the basal sedimentary layer above  
lengths in mm



$l_0 = \text{sum of individual segment lengths} = 123 \text{ mm}$

$$e = \frac{l_f - l_0}{l_0} = \frac{89 - 123}{123} = \frac{-34}{123} = \boxed{-0,276} \quad \text{NO UNITS}$$



# Stretched belemnite

This fossil, discovered in folded rocks in the western Alps by Albert Heim in the nineteenth century (Milnes, 1979), was stretched into an array of rigid shell fragments of approximately equal size. Spaces that developed during deformation were simultaneously filled by calcite. The original length ( $l_0$ ) of the belemnite fossil can be determined by measuring and summing the widths of the individual shell fragments. The final length ( $l_f$ ) of the belemnite is simply the total length of the fossil in its present state, including the calcite filling.

$$l_0 = 82 \text{ mm}, l_f = 185 \text{ mm}$$

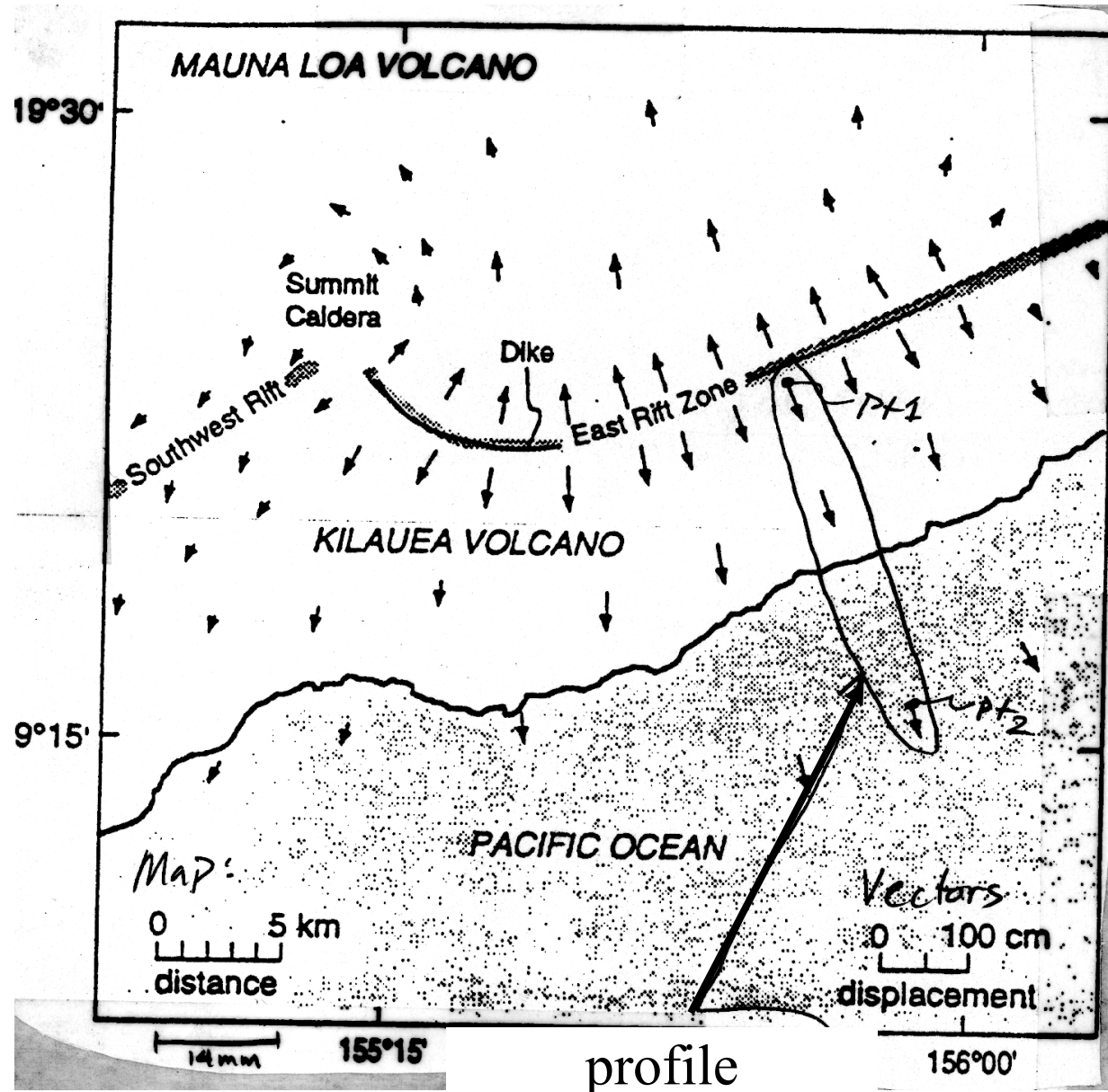
$$e = ?$$

$$s = ?$$



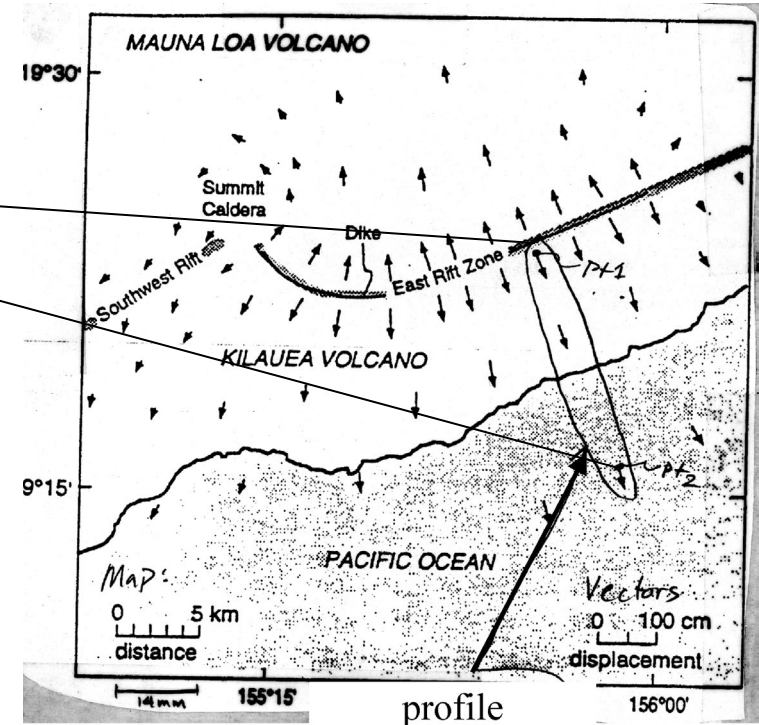
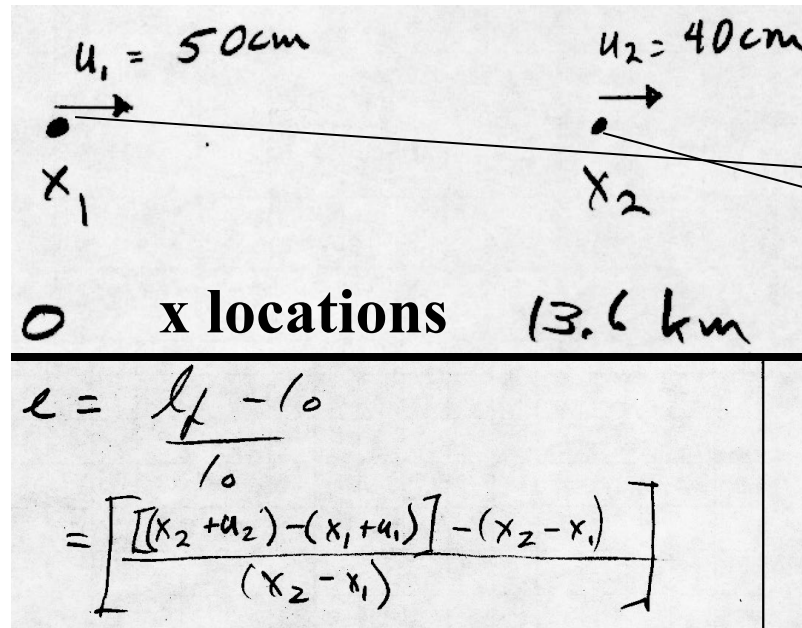
# Deformation and displacement gradients

Displacement vectors caused by dike inflation at Kilauea



# Consider a profile from point 1 to point 2:

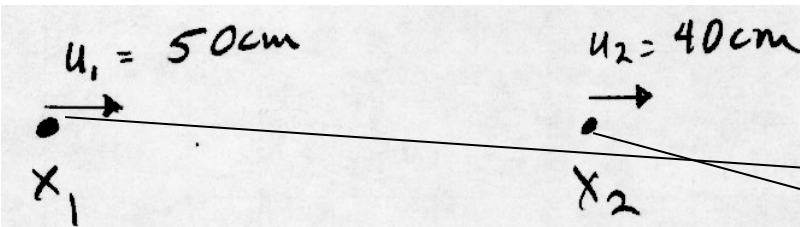
$u$  is velocity.  $x$  and  $u$  are positively increasing to the right



$$\frac{\Delta u}{\Delta x} = \frac{u_2 - u_1}{x_2 - x_1}$$

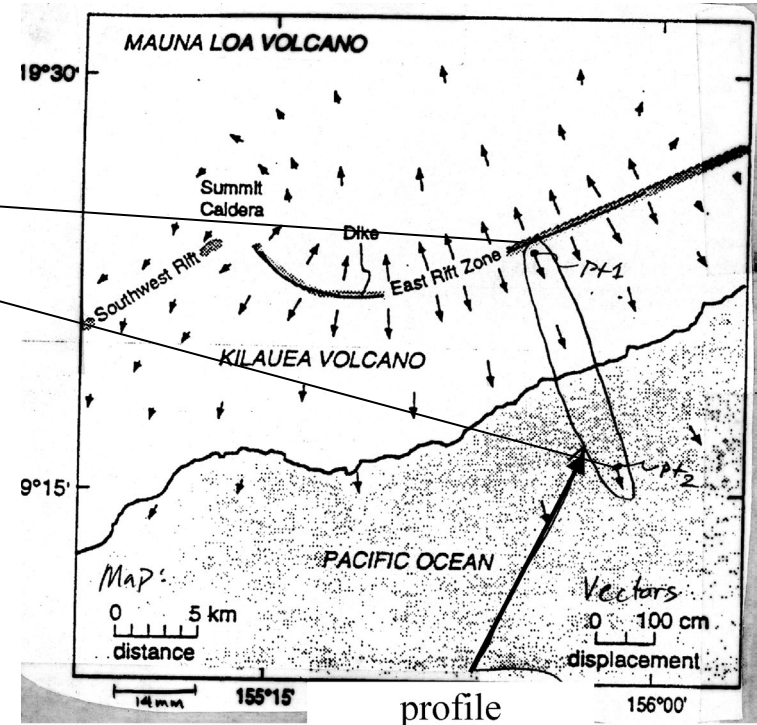
# Consider a profile from point 1 to point 2:

$u$  is velocity.  $x$  and  $u$  are positively increasing to the right



$x$  locations 13.6 km

$$\begin{aligned}
 \epsilon &= \frac{l_f - l_o}{l_o} \\
 &= \left[ \frac{[(x_2 + u_2) - (x_1 + u_1)] - (x_2 - x_1)}{(x_2 - x_1)} \right] \\
 &= \left[ \frac{[(13600\text{m} + 0.4\text{m}) - (0 + 0.5\text{m})] - (13600\text{m} - 0)}{13600 - 0} \right] \\
 &= \frac{[13600.4\text{m} - 0.5\text{m}] - 13600\text{m}}{13600} \\
 &= \frac{13599.9\text{m} - 13600\text{m}}{13600\text{m}} = - \\
 &= \frac{-0.1\text{m}}{13600\text{m}} = -7.4 \times 10^{-6} \quad \text{No units}
 \end{aligned}$$



$$\begin{aligned}
 \frac{\Delta u}{\Delta x} &= \frac{u_2 - u_1}{x_2 - x_1} \\
 \frac{0.4\text{m} - 0.5\text{m}}{13600\text{m} - 0\text{m}} &= \frac{-0.1\text{m}}{13600\text{m}}
 \end{aligned}$$

Same result

# Deformation rates

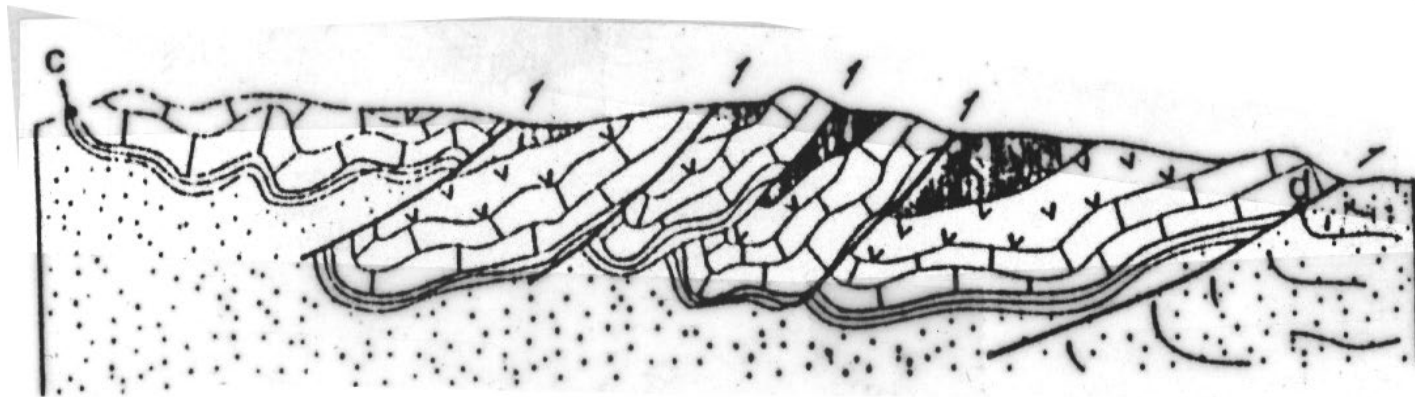
If we take the Kilauea example as a representative geologic deformation rate (and it is), how long would it take to build a structure like that shown below?

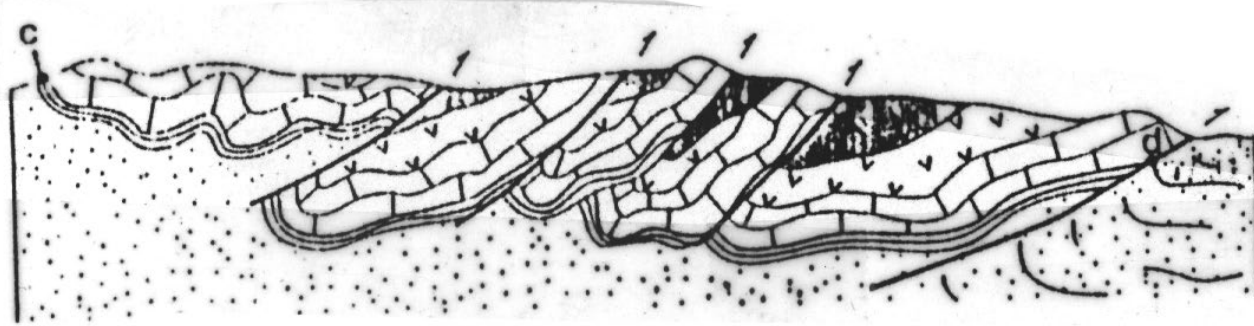
For Kilauea, we got  $-7.4 \times 10^{-6} = e$  over 20 yrs

to the contraction rate,  $e = \frac{-7.4 \times 10^{-6}}{20 \text{ yr}} = \boxed{-3.7 \times 10^{-7} \text{ yr}^{-1}}$

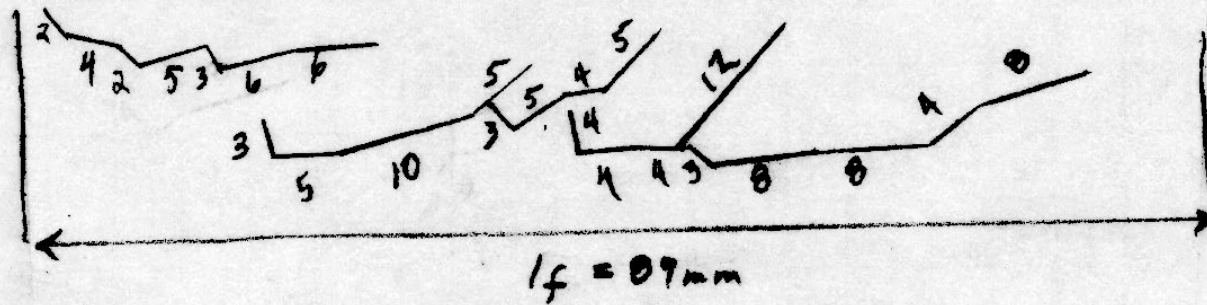
$-3.7 \times 10^{-7} \frac{1}{\text{yr}} = \frac{1 \text{ yr}}{365 \text{ days}} \cdot \frac{1 \text{ day}}{24 \text{ hrs}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} =$

$-1.2 \times 10^{-14} \text{ sec}^{-1}$





Line segments approximating the basal sedimentary layer above  
lengths in mm



$l_0 =$  sum of individual segment lengths  $= 123$  mm

$$e = \frac{l_f - l_0}{l_0} = \frac{89 - 123}{123} = \frac{-34}{123} = \boxed{-0,276} \text{ No units}$$

We want time, so we divide  $e$  by  $\dot{e}$ :

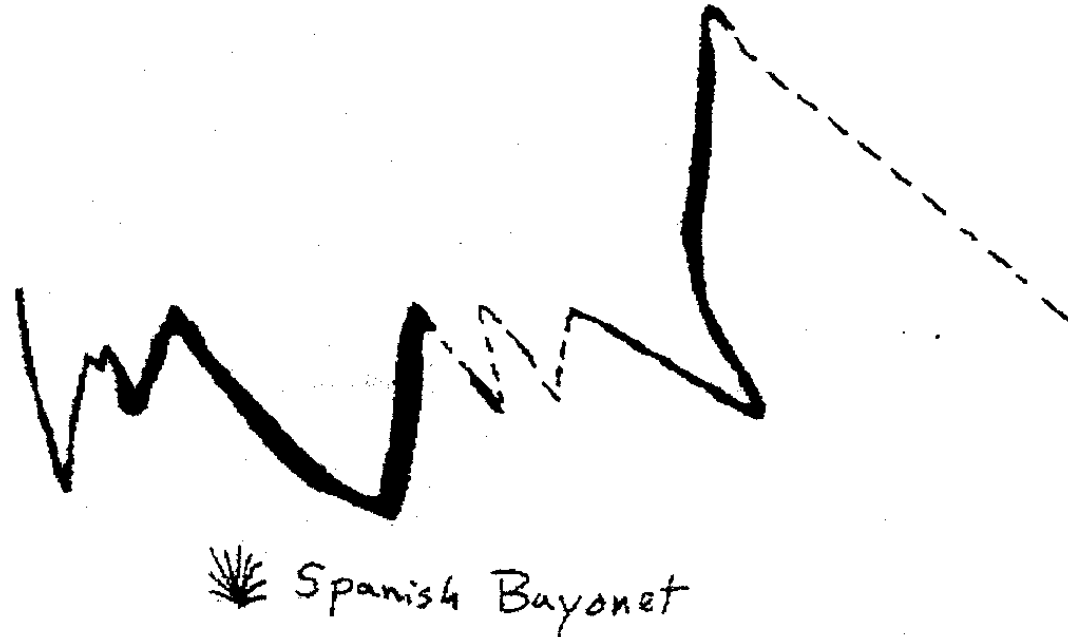
$$\frac{-0,276}{-3,7 \times 10^{-7} \text{ yr}^{-1}} = 750,000 \text{ yrs!}$$

$7.5 \times 10^5 \text{ yr}$

**Folds!**



Folded quartzite layers  
within the Maverick shale  
Barnhardt Canyon, AZ



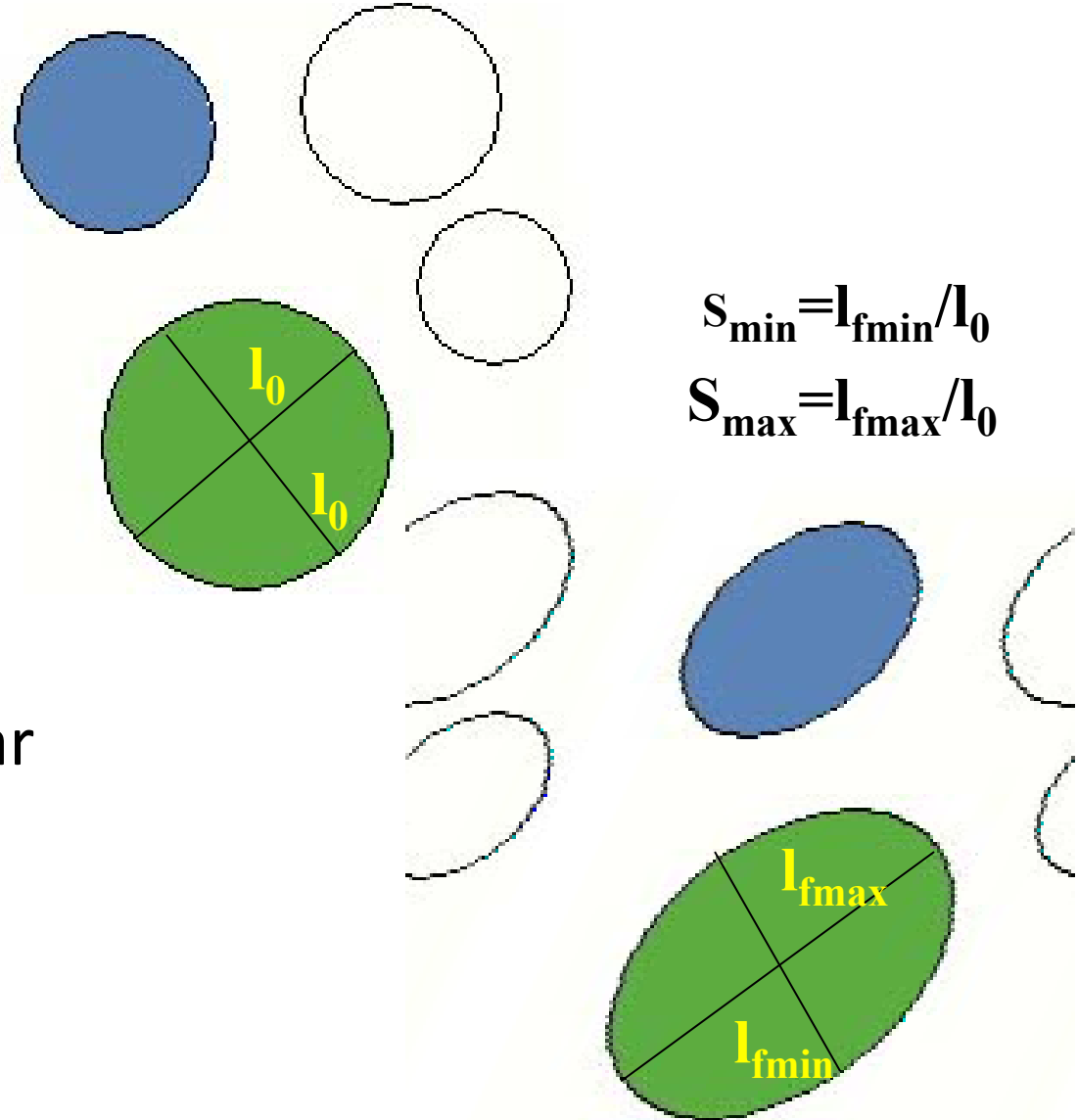
**Determine the magnitude of shortening ( $\epsilon$ ) of this bed assuming that it was originally planar**

**If a reasonable shortening rate is  $-1 \times 10^{-7}$ /yr, how long would it take to make these folds?**

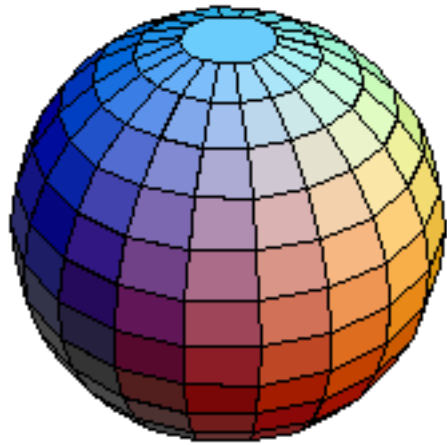


# Moving from 1 to 2 to 3 dimensional deformation

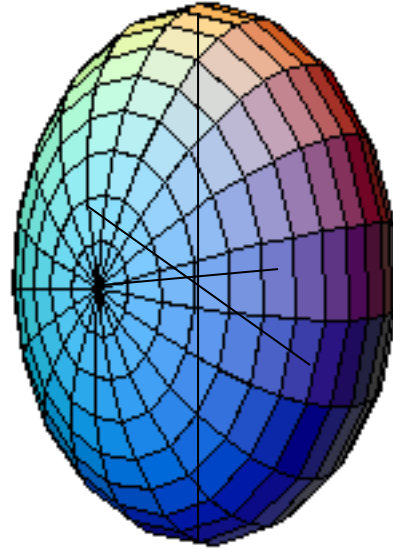
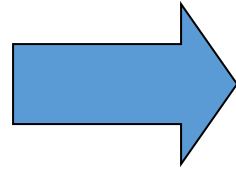
- E and s as we have defined them in the last two lectures are 1 dimensional (measured along  $l_f$ ).
- In a deformed material; however, we can define the minimum and maximum stretches and they will be perpendicular



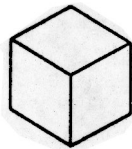
# Principal stretches



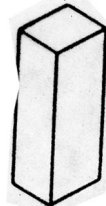
**Sphere**



**Ellipsoid**

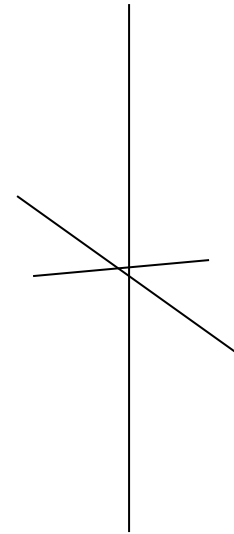


**Cube**



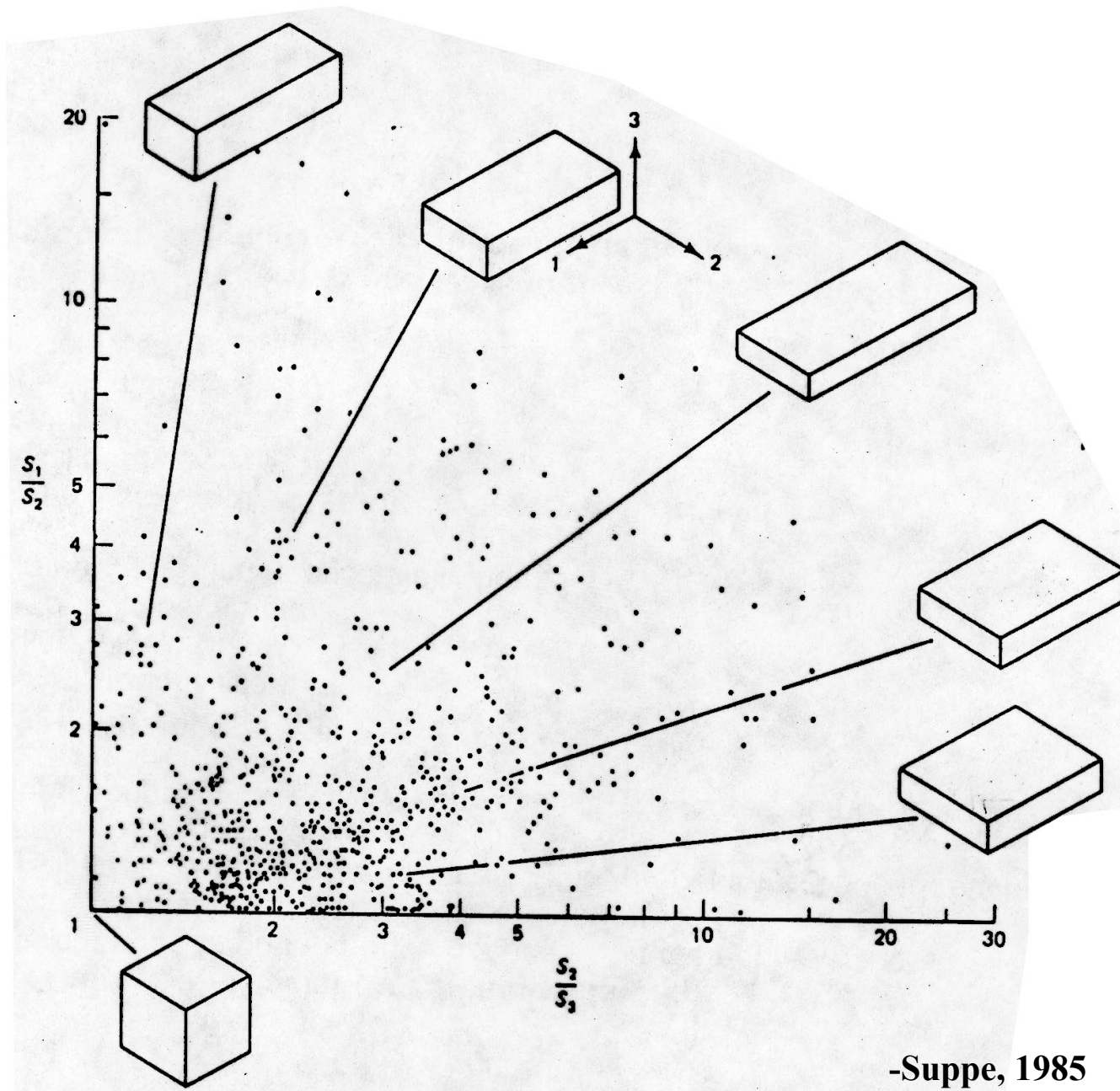
**Prism**

**In 3D,  $S_1$  is max,  
 $S_3$  is min, and  $S_2$  is  
intermediate**



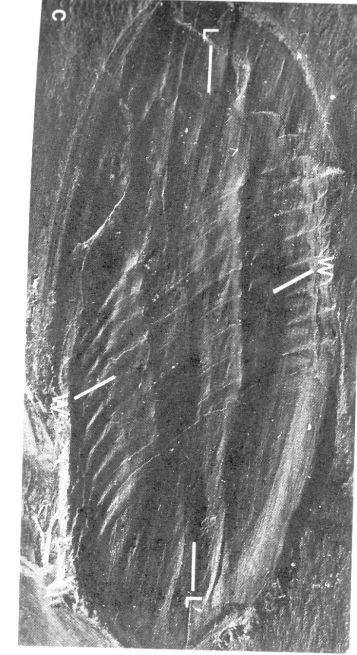
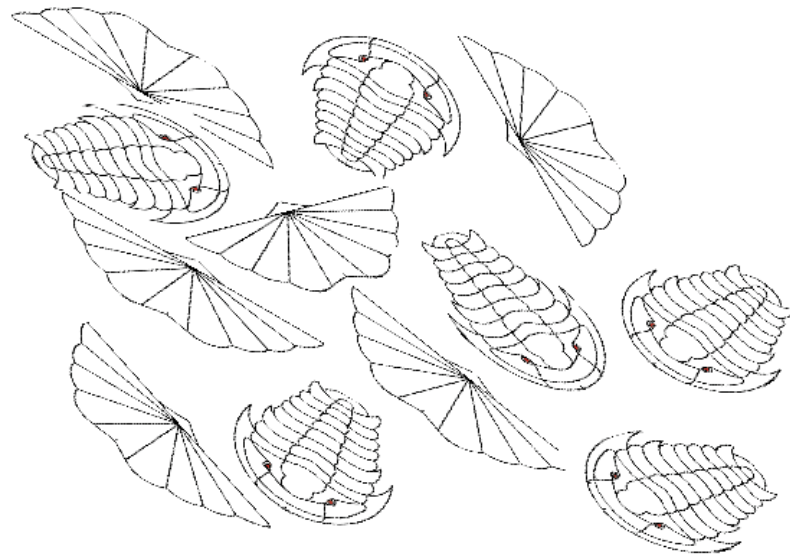
# Measured stretch ratios in rocks from around the world

“Constriction”

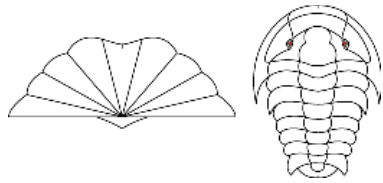


“Flattening”  
More common

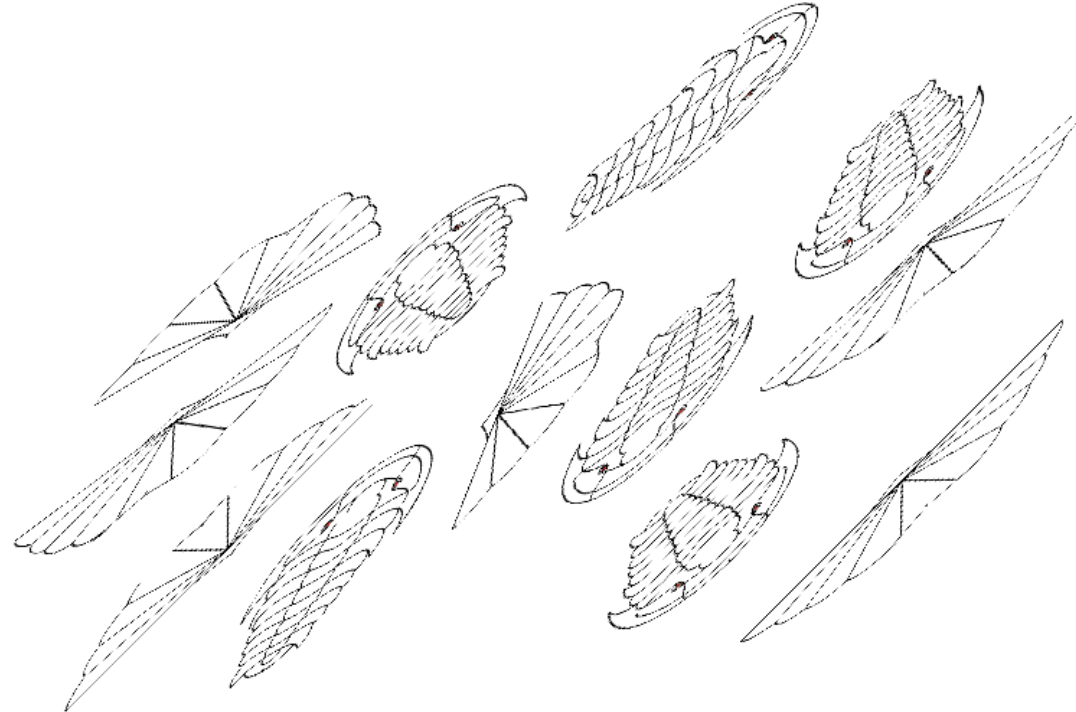
-Suppe, 1985



**Deformed  
trilobites  
do exist!**



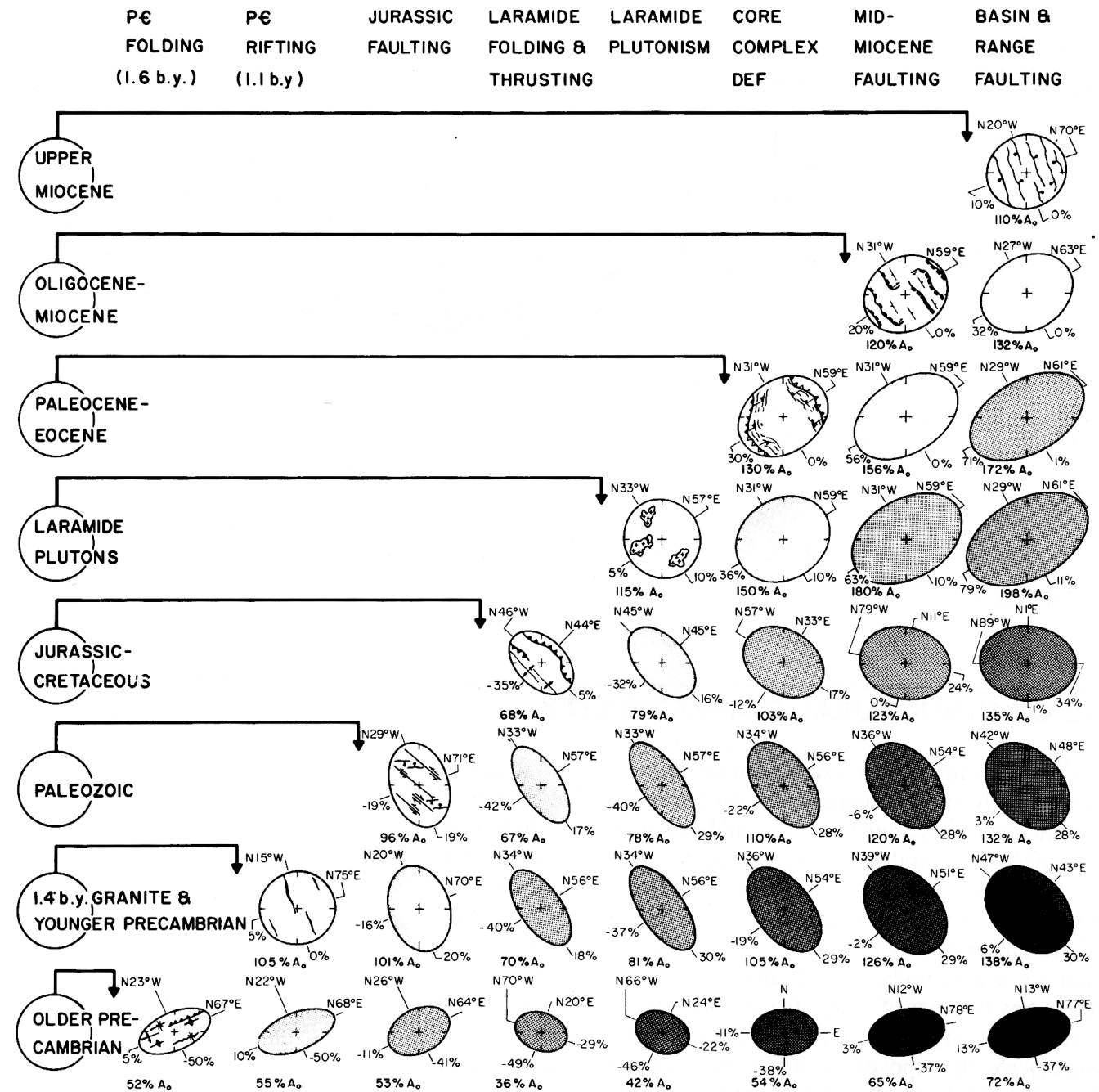
**Draw the  
stretch  
ellipse for  
each**



# Progressive strain

## ROCK ASSEMBLAGES

## DEFORMATIONS



# History of regional deformation in southern Arizona